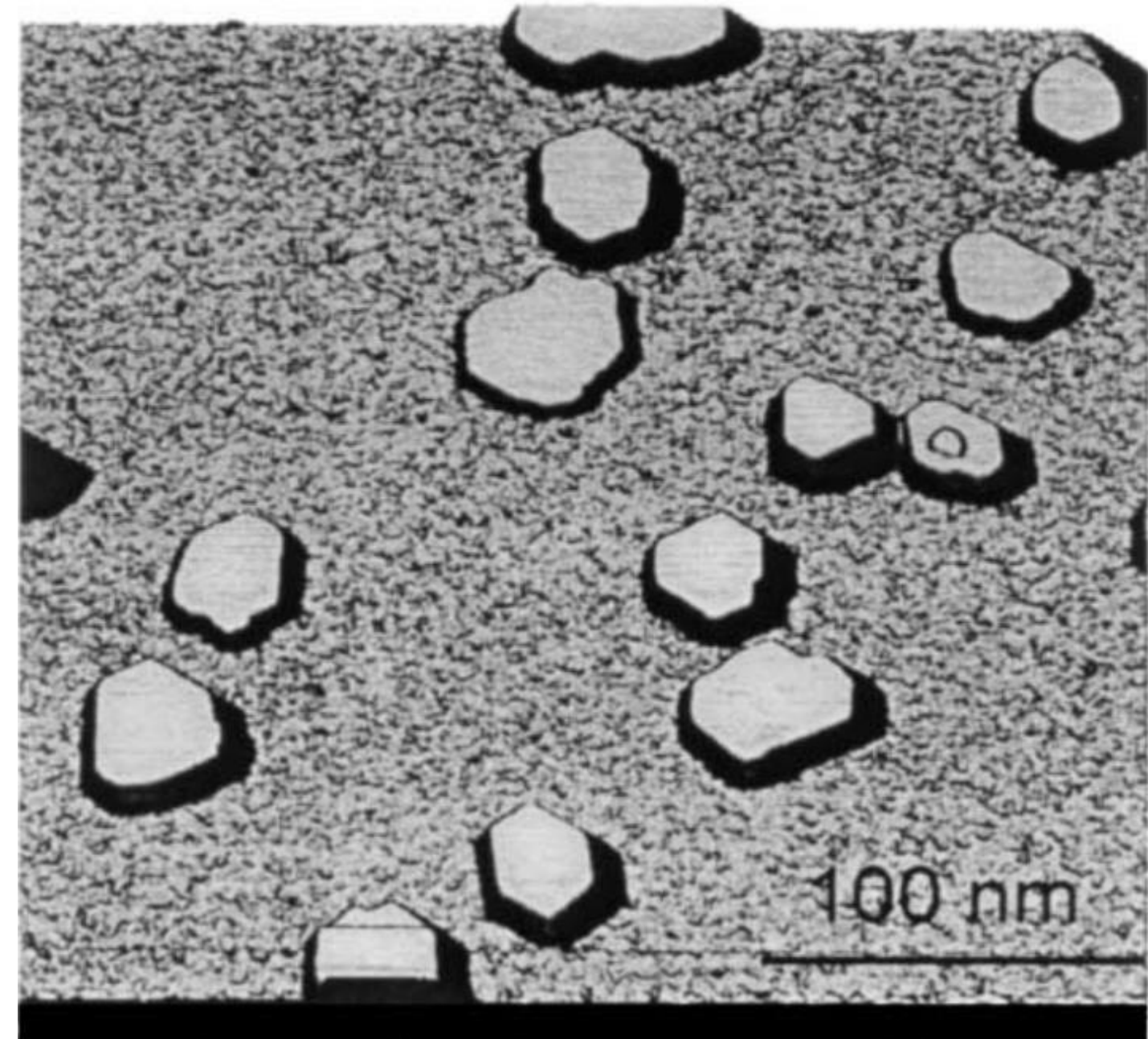


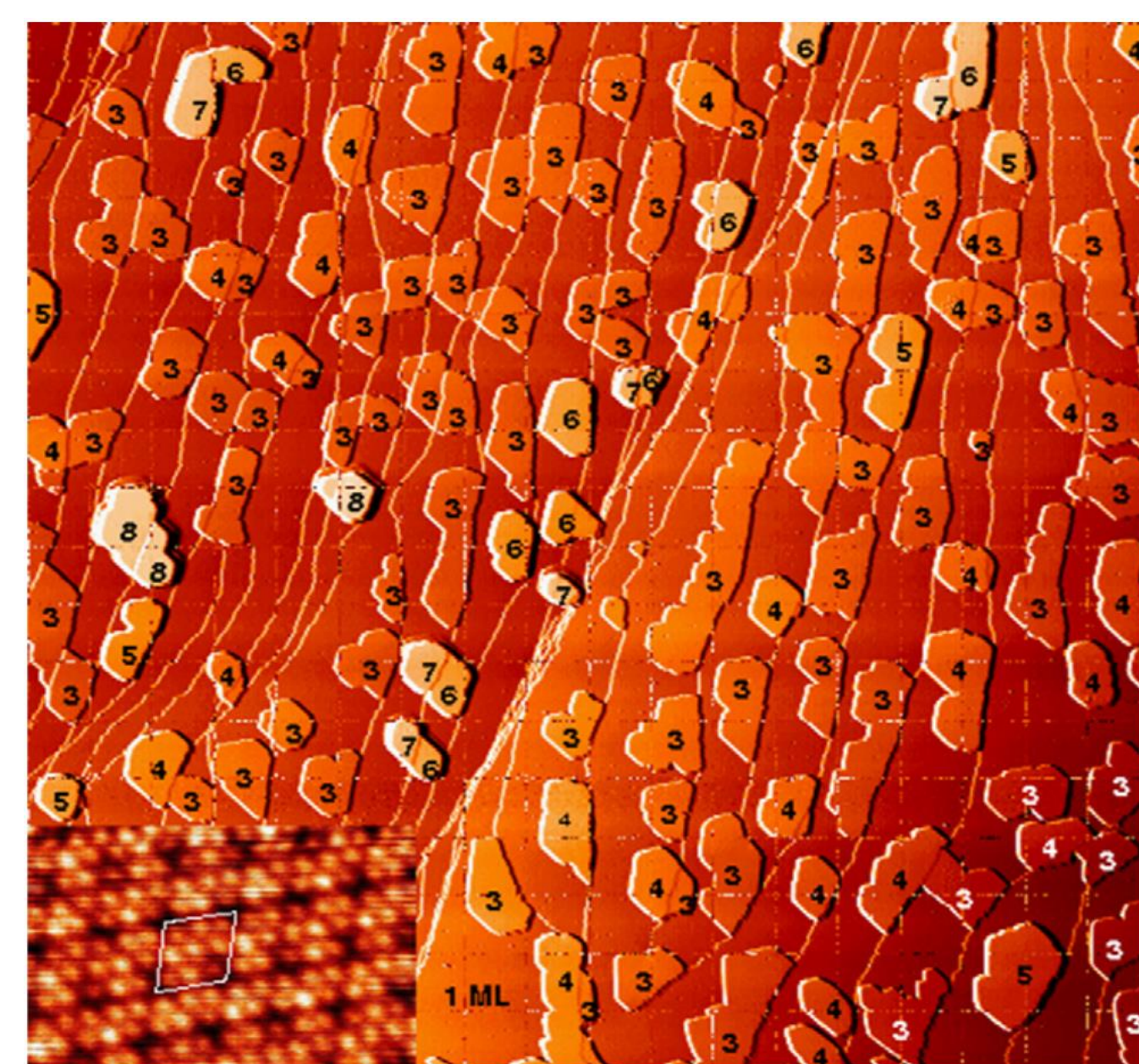
## ABSTRACT

We present computed evolution (in the annealing stage) of the quantum Pb and Ag nanoislands that form on an ultrathin epitaxial film during non-traditional two-step growth (A.R. Smith et al., Science 273, 226 (1996)). We find the complicated spectra of a metastable and stable “magic” island heights, the surface diffusion pathways that lead to a flat-top 2D islands having these heights, and the coarsening rules that underlie the morphological evolution resulting in the “survival of the fittest” among nanoislands of different heights and sizes.

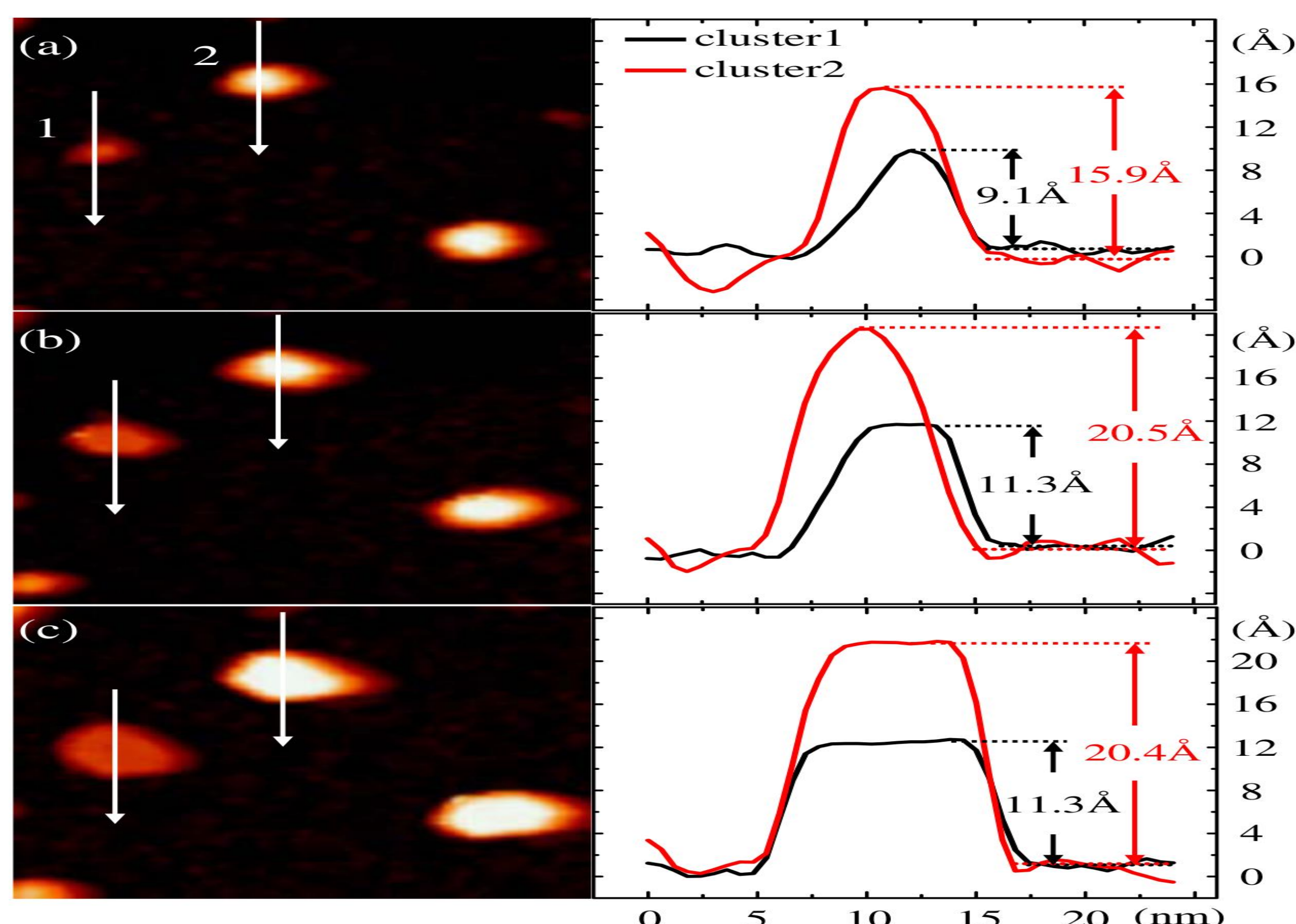
## EXPERIMENT



W.B. Su et al., PRL 86, 5116 (2001)



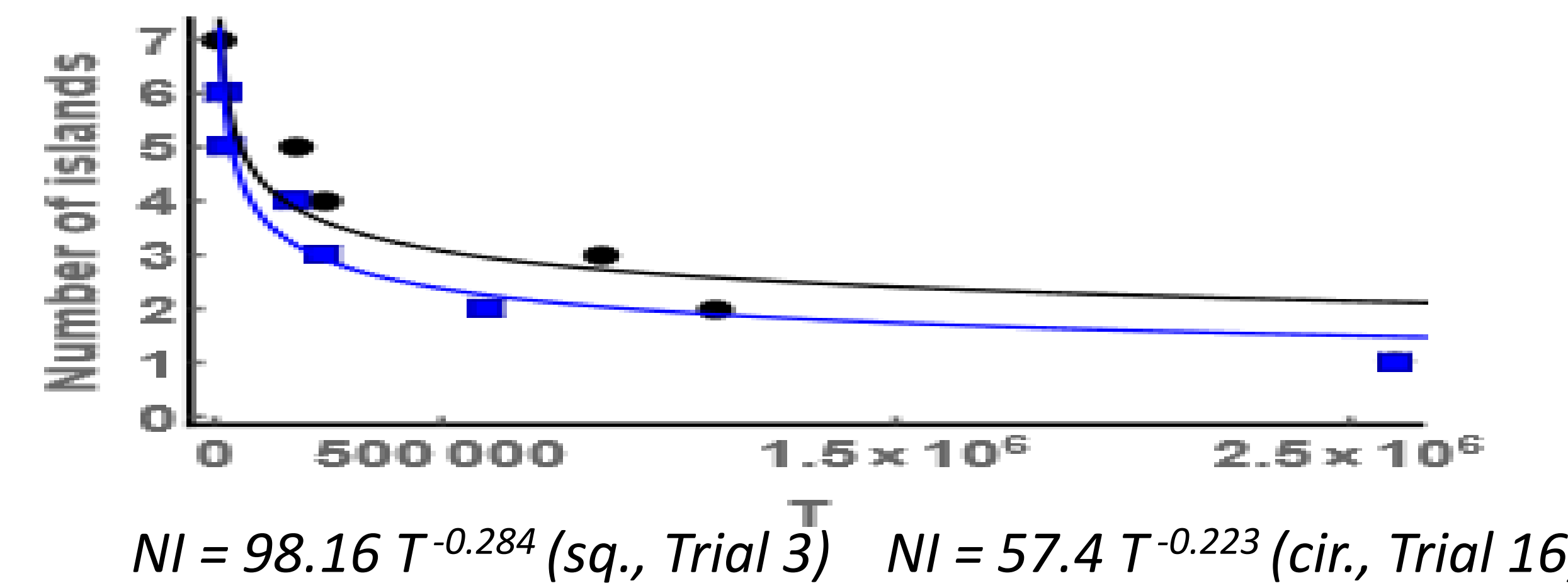
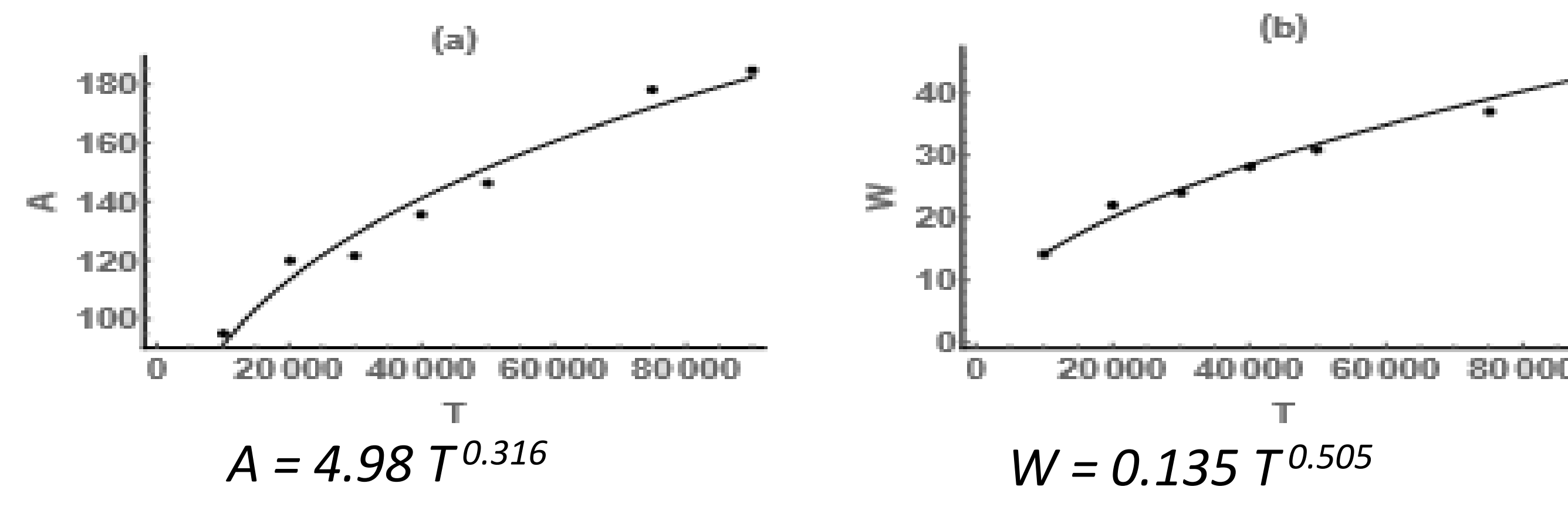
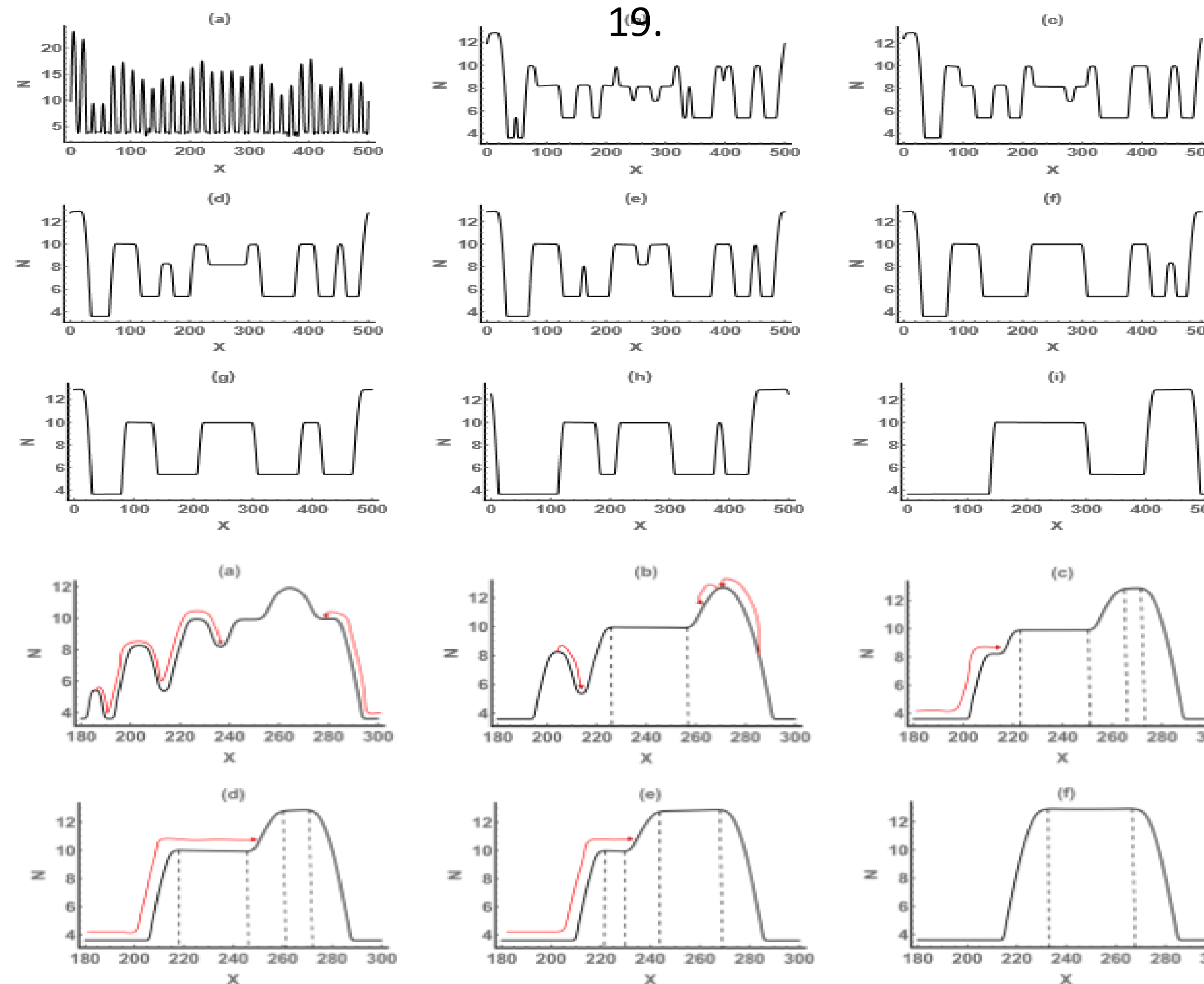
F. Calleja et al., Applied Surface Science 254, 12-15 (2007)



W.B. Su et al., J. Phys. D: Appl. Phys. 43, 013001 (2010)

## Our model: Ag(110)

“Magic” nanoisland heights (N, in atom monolayers) from the experiment (Y. Han et al., Materials 3, 3965 (2010)): 2, 4, 6, 8?, 10?,...; from our theory: 2, 4, 5, 7, 8, 10, 13, 16, 19.



## KEY EQUATIONS OF THE MODEL

$$h_t = \sqrt{1 + h_x^2 + h_y^2} D \nabla_s^2 (\mu + \Sigma) \quad (1)$$

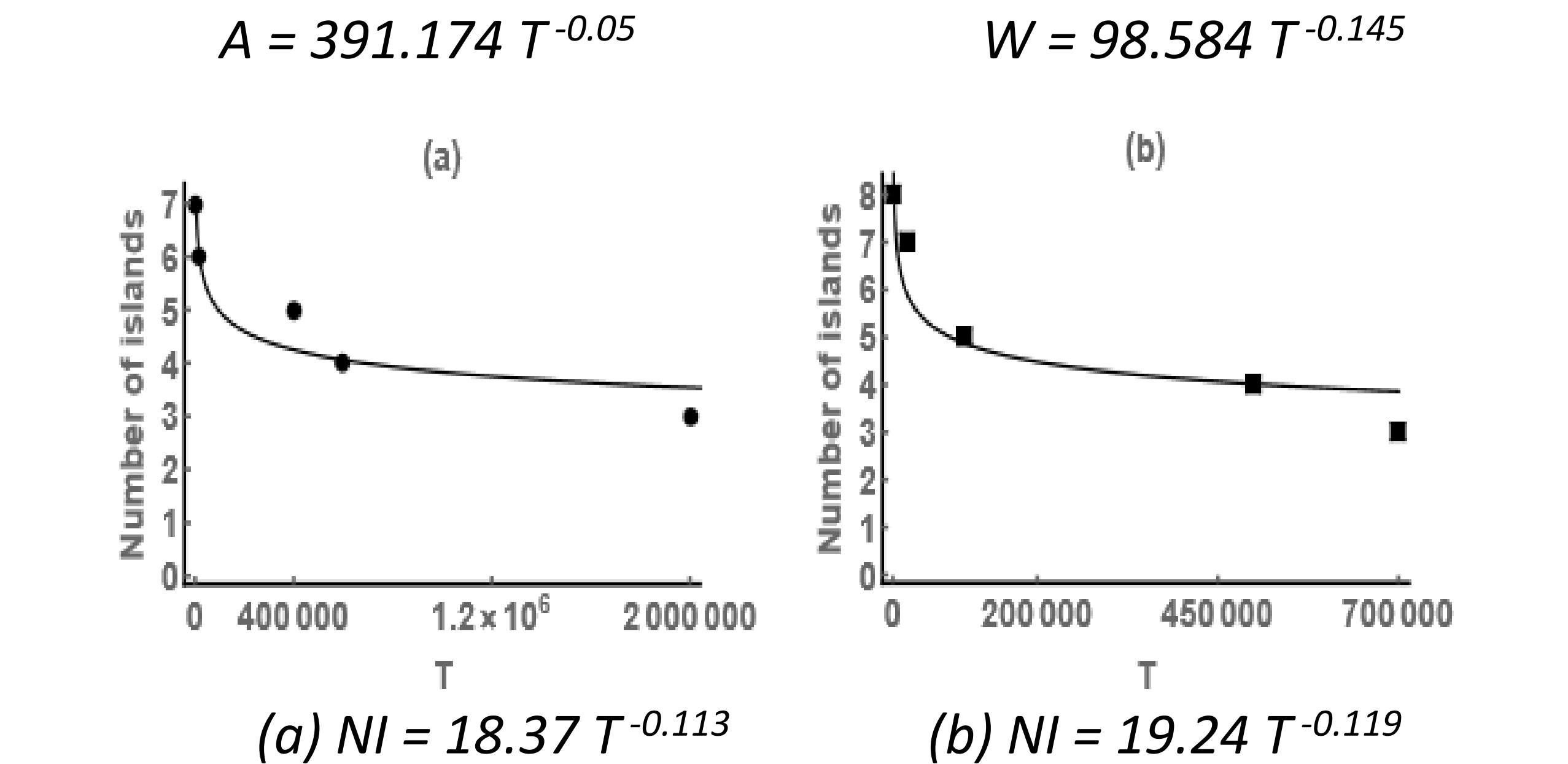
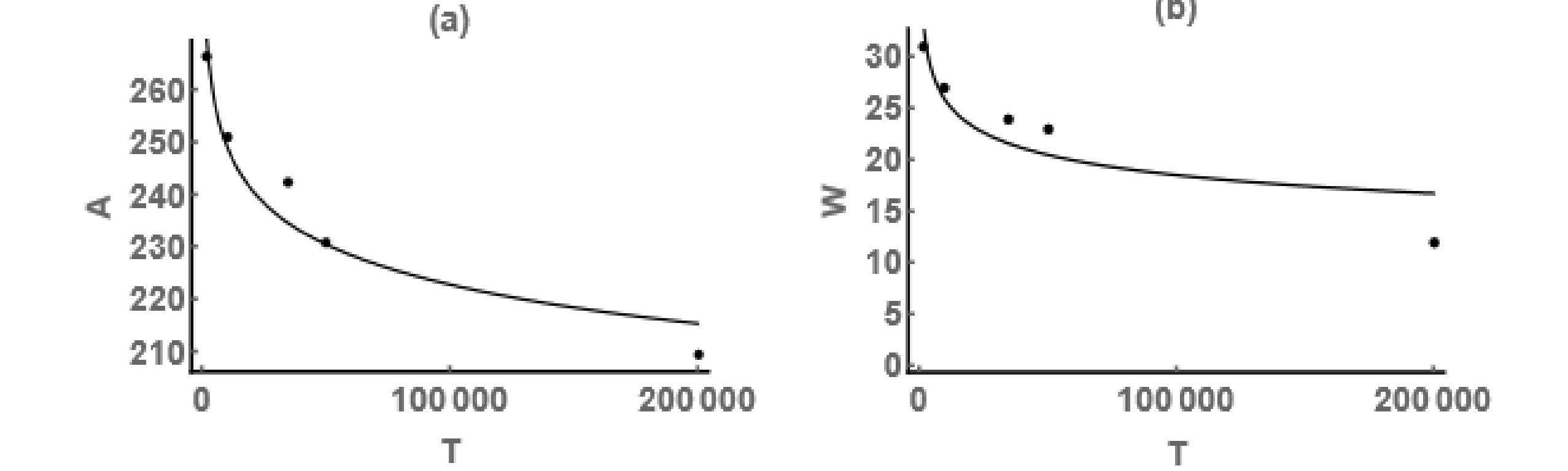
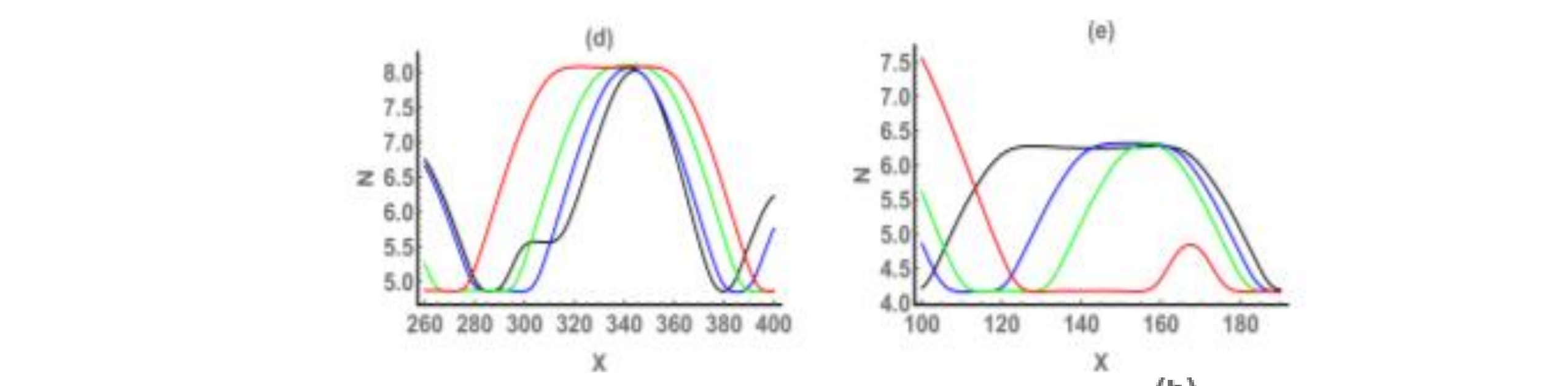
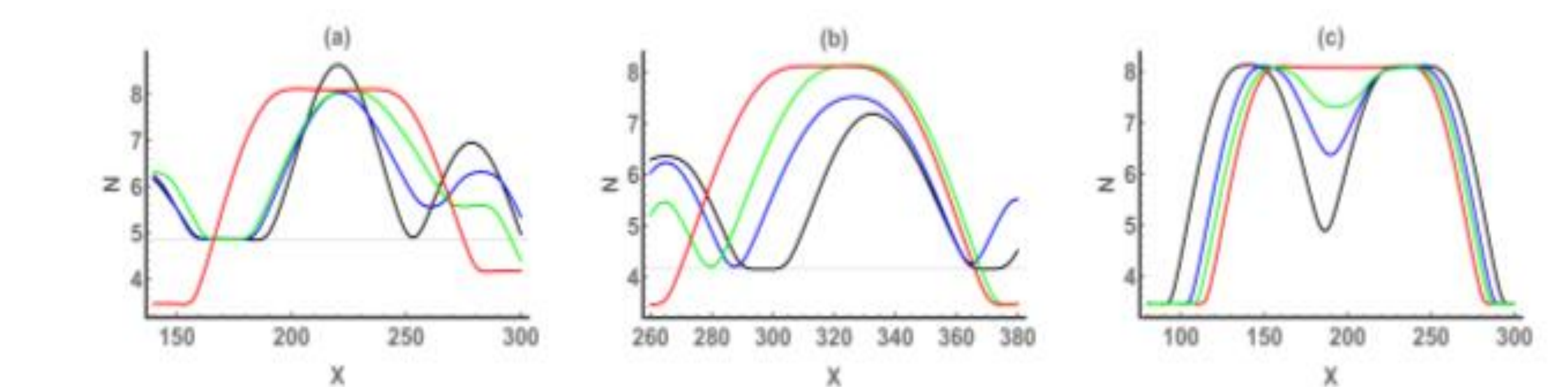
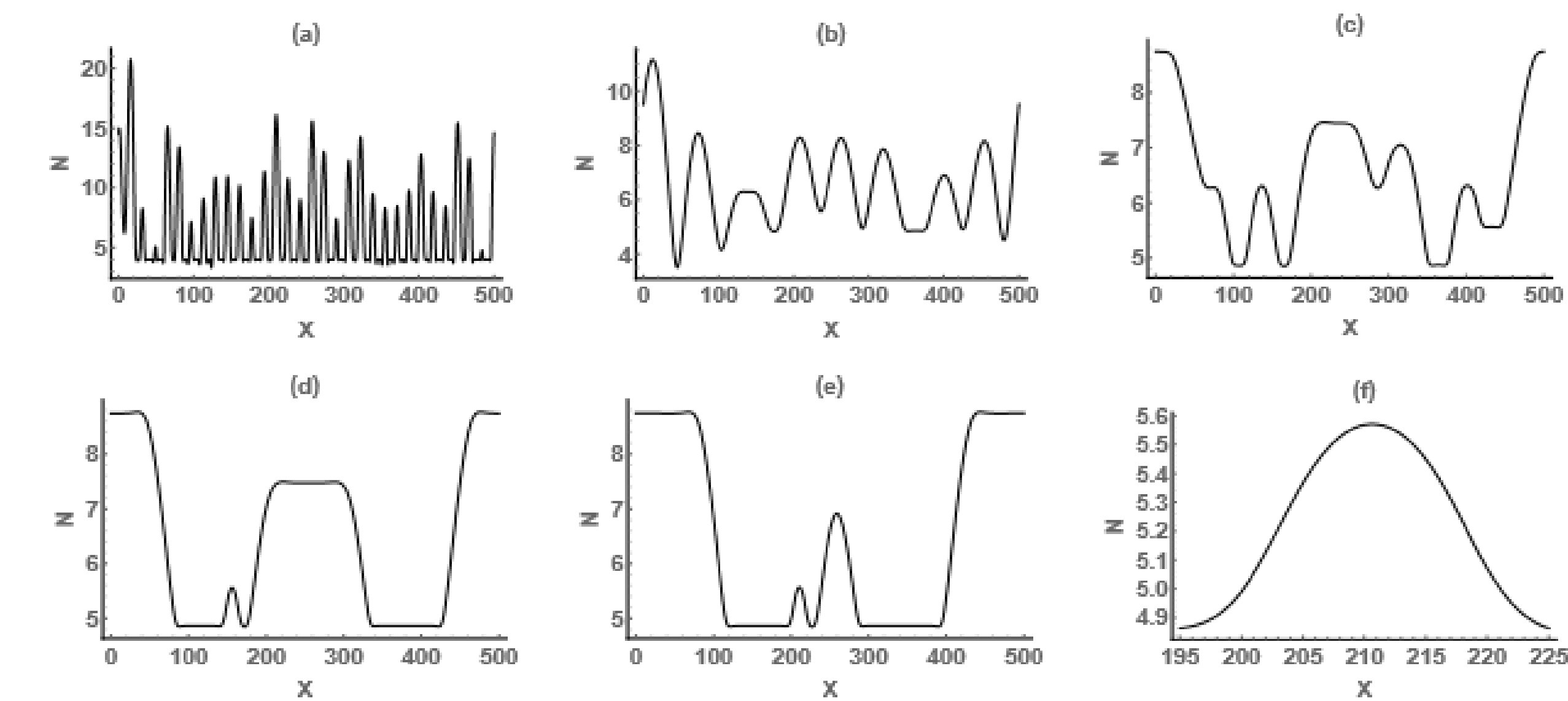
$$\mu = \gamma(h) \kappa + n_3 \frac{d\gamma(h)}{dh} \quad (2)$$

$$\gamma(h) = \gamma_{bf} + \frac{g_0 s^2}{(h+s)^2} \cos \omega_1 h \cos \omega_2 h - \frac{g_1 s}{h+s} \quad (3)$$

$h$  is the film height,  $\mu$  the chemical potential,  $\gamma$  the surface energy

## Our model: Pb(111)

“Magic” nanoisland heights (N, in atom monolayers) from the experiment (M.M. Ozer et al., J. Low Temp. Phys. 157, 221 (2009)): 6, 8, 10, 12, 14(15), 17, 19, 21; from our theory: 2, 4, 6, 7, 9, 11, 12, 14, 16, 17, 19.



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